

## **Mathematics**

## Year 9

## What are the aims and intentions of this curriculum?

The aim of our Key Stage 3 Curriculum is to consolidate the numerical and mathematical capability and skills learnt from key stage 2 and to extend students' understanding of the number system and place value to include decimals, fractions, powers and roots. The curriculum also seeks to equip students with the knowledge to be able to make generalisations about the number system that will help them to make the necessary connections between mathematical topics and voids reteaching when developing concepts in isolation. It also seeks to develop fluent understanding of the axioms and structures of number that are fundamental to mathematics which underpins the understanding of algebraic notations developed in this year and in the subsequent years. The KS3 Curriculum also aims to equip Students to apply algebraic reasoning in new contexts such as Geometry, and to also make linkage to different interpretations of fractions and be introduced to ratio. To provide students with a holistic experience, prepare them for future success, help them aspire and value mathematics, **Fersonal Social Health and tronomet (PSHC)** education and **Careers Education (CE)** are incorporated into the curriculum.

Term	Topics	Knowledge and key terms	Skills developed	Assessment
Summer 2	<ul> <li>Number</li> <li>Order of Operation</li> <li>Rounding, Approximation and estimation</li> <li>Factors and Multiples (HCF and LCM, Venn Diagram)</li> <li>Roots and Surds</li> <li>Indices</li> </ul>	<ul> <li>Students will be able to:</li> <li>Calculate accurately negative and positive numbers following BIDMAS</li> <li>Round numbers and Estimation calculations</li> <li>Work accurately with square, cubes and roots</li> <li>Identify primes, factors and multiples</li> <li>Complete prime factorisation Factors: families – using the factor tree Multiples: extended families (number of family members living together  Prime: Single parent – Mom and 1 child or Dad and 1  child </li> <li>Find HCF and LCM </li> <li>Optimise resources and eliminate wastage.</li> <li>Understand surd notation-Being Irrational Understand and work with questions involving surds including rationalising the denominator. Work with indices- Index laws </li> </ul>	<ul> <li>Select and use appropriate calculation strategies to solve increasingly complex problems</li> <li>Extend their understanding of the number system.</li> <li>Use conventional notation for the priority of operations, including brackets, powers, roots and reciprocals</li> <li>Recognise and use relationships between operations including inverse operations</li> <li>Appreciate the infinite nature of the sets of integers, real and rational numbers.</li> <li>calculate exactly with fractions, surds and multiples of π; simplify surd expressions involving squares (e.g. v12 = v(4 × 3) = v4 × v3 = 2v3) and rationalise denominators</li> <li>Use problem solving strategies to find solutions</li> </ul>	<ul> <li>All pupils will be sitting an End of term assessment.</li> <li>Pupils will be assessed additionally as best seen fit by their subject teacher.</li> <li>Mathswatch</li> <li>Group work Class discussions Targeted Questioning</li> </ul>

•	Standard form and its	
	applications	Calculate with Standard form
≻	Algebra	
		• Distinguish between expressions, equations,
•	Algebraic indices	formulae and identities.
•	Expression, equations and Formulae	• Factorise expressions into a single bracket
•	Algebraic simplification	• Factorise Quadratic expressions when a=1
		Solve equations involving brackets and
		<ul><li>numerical fractions.</li><li>Use algebraic methods to solve linear</li></ul>
•	Algebraic Expansion and Factorisation	equations in one variable (including all forms
		that require rearrangement)
		• Expand products of one or two or three
		<ul><li>binomials</li><li>Substitute numbers into formulae.</li></ul>
		Rearrange formulae.
		• Substitute values in expressions, rearrange
		and simplify expressions, and solve
		equations
•	Linear sequences	
•	Quadratic Sequences	
		• Find a general formula for the nth term of an arithmetic sequence.
		<ul> <li>Determine whether a particular number is a</li> </ul>
		term of a given arithmetic sequence.
		Solve problems using geometric sequences.
		• Work out terms in Fibonnaci-like sequences.

- Calculate with and interpret standard form A × 10<sup>n</sup>, where 1 ≤ A < 10 and n is an integer
- substitute numerical values into formulae and expressions, including scientific formulae
- understand and use the concepts and vocabulary of expressions, equations, formulae, <u>identities</u>, inequalities, terms and factors
- understand and use standard mathematical formulae; rearrange formulae to change the subject
- know the difference between an equation and an identity; argue mathematically to show algebraic expressions are equivalent, and use algebra to support and construct arguments and proofs
- where appropriate, interpret simple expressions as functions with inputs and outputs; ; interpret the reverse process as the 'inverse function'; interpret the succession of two functions as a 'composite function' (the use of formal function notation is expected)
- generate terms of a sequence from either a term-to-term or a position-toterm rule
- Make and test conjectures about patterns and relationships; look for proofs or counter-examples

		Predicting	<ul> <li>recognise and use sequences of triangular, square and cube numbers, simple arithmetic progressions, Fibonacci type sequences, quadratic sequences, and simple geometric progressions (r<sup>n</sup> where n is an integer, and r is a rational number &gt; 0 or a surd) and other sequences</li> <li>deduce expressions to calculate the nth term of linear and quadratic sequences</li> <li>Model situations or procedures by translating them into algebraic expressions</li> <li>Solve problems involving linear sequences in a variety of contexts</li> <li>Students begin to appreciate that writing with algebra applies the rules of arithmetic to unknown numbers which are represented as letters.</li> </ul>	
Autumn 1	<ul> <li>Algebra</li> <li>Equation of straight-line graphs</li> </ul>	<ul> <li>Students will be able to:</li> <li>Work with Coordinates in all four Quadrants</li> <li>Identify the equations of horizontal and vertical lines</li> <li>Plot coordinates from a rule to generate a straight line</li> <li>Finding the gradient and y intercept of a line and equations of straight line given the gradient and y intercept.</li> <li>Finding equations of parallel and perpendicular lines.</li> </ul>	<ul> <li>Make connections between number relationships, and their algebraic and graphical representations</li> <li>Identify key features of a linear graph</li> <li>identify and interpret gradients and intercepts of linear functions graphically and algebraically</li> <li>plot graphs of equations that correspond to straight-line graphs in the coordinate plane; use the form y = mx + c to identify parallel and perpendicular lines; find the equation of the line through two given points or through one point with a given gradient</li> </ul>	<ul> <li>All pupils will be sitting an End of term assessment.</li> <li>Pupils will be assessed additionally as best seen fit by their subject teacher.</li> <li>Mathswatch</li> <li>Mathswatch</li> <li>Group work Class discussions</li> </ul>
	<ul> <li>Solving equations</li> </ul>	<ul> <li>Solving Simultaneous equations</li> </ul>	<ul> <li>solve two simultaneous equations in two variables (linear/linear or linear/quadratic) algebraically; find approximate solutions using a graph</li> </ul>	Targeted Questioning

		Introduction to KS4 content: Solve     simultaneous equations algebraically and		
		simultaneous equations algebraically and graphically.		
		graphically.		
	<ul> <li>Laws of Indices (More</li> </ul>			
	Complex)	• Understand, derive and use the rules of		
		indices with integer values		
		<ul> <li>Apply the laws of Indices with Algebra-</li> </ul>		
		including fractional and negative indices.		
Autumn 2	Handling Data	Students will be able to:		• At the end of each unit
	Graphs, Charts for both	• Construct and use back-to-back stem	• Describe, interpret and compare observed	there will be a unit test.
	Grouped and ungrouped	and leaf diagrams.	distributions of a single variable through:	
	data	Construct and use frequency polygons	appropriate graphical representation	There will be online
		and pie charts.	involving discrete, continuous and grouped	assessments for each
	<ul> <li>Statistical Measures</li> </ul>	<ul> <li>Plot and interpret time series graphs.</li> </ul>	data; and appropriate measures of central	topic covered.
		<ul> <li>Use trends to predict what might</li> </ul>	tendency (mean, mode, median) and spread	
	Averages from tables and     Graphs	happen in the future.	(range, consideration of outliers)	
	Graphs	<ul> <li>Plot and interpret scatter graphs.</li> </ul>	Construct and interpret appropriate tables,	<ul> <li>All pupils will be sitting an End of term</li> </ul>
	<ul> <li>Statistical diagrams 1</li> </ul>	Determine whether or not there is a	charts, and diagrams, including frequency	assessment.
	Time series	linear relationship between two	tables, bar charts, pie charts, and pictograms for categorical data, and vertical line (or bar)	assessment.
	Scatter graphs	variables.	charts for ungrouped and grouped numerical	Pupils will be assessed
	<ul> <li>Line of best fit</li> </ul>	Draw a line of best fit on a scatter     graph	data.	additionally as best
	<ul> <li>Averages and range</li> </ul>	<ul><li>graph.</li><li>Use the line of best fit to predict values.</li></ul>	Describe simple mathematical relationships	seen fit by their subject
	Statistical diagrams 2	<ul> <li>Decide which average is best for a set of</li> </ul>	between two variables (Bivariate data) in	teacher.
		data.	observational and experimental contexts	
		<ul> <li>Estimate the mean and range from a</li> </ul>	and Illustrate this using scatter graphs.	<ul> <li>Mathswatch</li> </ul>
		grouped frequency table.	<ul> <li>Identify possible primary or secondary</li> </ul>	
		<ul> <li>Find the modal class and the group</li> </ul>	sources; determine the sample size and	Group work
		containing the median.	most appropriate degree of accuracy.	Class discussions
		<ul> <li>Construct and use two-way tables.</li> </ul>		Targeted Questioning
		Choose appropriate diagrams to display		
		data.		
		<ul> <li>Recognise misleading graphs.</li> </ul>	<ul> <li>solve linear equations in one unknown</li> </ul>	
	Algebra		algebraically (including those with the	
			unknown on both sides of the equation); find	
	<ul> <li>Solving harder equations</li> </ul>	<ul> <li>Form and solve linear equations and</li> </ul>	approximate solutions using a graph	
		inequalities in one unknown, including those		
		where the unknown appears on both sides		
	<ul> <li>Inequalities</li> </ul>			

Spring 1 <ul> <li>Number</li> <li>Fraction, Decimal and Percentages</li> <li>Convert between fractions, decimals and percentages greater than 100%</li> <li>Use percentages greater than 100%</li> <li>Express one quantity is a percentage of another</li> <li>Increase and decrease a quantity by a given percentage</li> <li>Find the original quantity using its final amount and percentage change and reverse percentage</li> <li>Solve problems involving percentage change and reverse percentage</li> <li>Virite, simplify and compare ratios</li> <li>Percentaging</li> <li>Solve problems involving ratio and proportion</li> <li>Solve problems involving ratio and proportion</li> <li>Solve problems involving ratio and proportion as equality of ratios and romains involving ratio and proportion as equality of ratios and ratios apply ratio to radictions and to linear functions</li> <li>Solve problems involving ratio and procentage since and to linear functions</li> <li>Solve problems involving ratio and percentage as number of parts per hundred; interpret percentages an function or a decima, and interpret these multiplicatively; express on equantity as a percentage inducing explased in the mumber endi</li></ul>		<ul> <li>Rearrange and solve linear equations and inequalities given in any form, including those involving fractions and brackets</li> </ul>	<ul> <li>solve linear inequalities in one or two variable(s); represent the solution set on a number line</li> </ul>	
problems, and simple interest including in	Fraction, D Percentage     Percentage	<ul> <li>Convert between fractions, decimals and percentages (review Year 7)</li> <li>Use percentages greater than 100%</li> <li>Express one quantity as a percentage of another</li> <li>Increase and decrease a quantity by a given percentage</li> <li>Find the original quantity using its final amount and percentage change</li> <li>Solve problems involving percentage change</li> <li>Write, simplify and compare ratios</li> <li>Pharmacist making a mixture (medication) for a given patient</li> <li>Convert between currencies and measures</li> <li>Recognise and use direct proportion</li> <li>Solve problems involving ratio and proportion.</li> </ul>	<ul> <li>system.</li> <li>extend and formalise their knowledge of ratio and proportion in working with measures and geometry, and in formulating proportional relations algebraically</li> <li>identify and work with fractions in ratio problems</li> <li>interpret fractions and percentages as operators</li> <li>use ratio notation, including reduction to simplest form</li> <li>divide a given quantity into two parts in a given part:part or part:whole ratio; express the division of a quantity into two parts as a ratio; apply ratio to real contexts and problems (such as those involving conversion, comparison, scaling, mixing, concentrations)</li> <li>express a multiplicative relationship between two quantities as a ratio or a fraction</li> <li>understand and use proportion as equality of ratios</li> <li>relate ratios to fractions and to linear functions</li> <li>define percentage as `number of parts per hundred¿; interpret percentages and percentage changes as a fraction or a decimal, and interpret these multiplicatively; express one quantity as a percentage of another; compare two quantities using percentages; work with percentages greater than 100%; solve problems involving percentage increase/decrease and original value</li> </ul>	<ul> <li>an End of term assessment.</li> <li>Pupils will be assessed additionally as best seen fit by their subject teacher.</li> <li>Mathswatch</li> <li>Group work</li> <li>Class discussions</li> </ul>

	<ul> <li>SSM</li> <li>Angles and trigonometry</li> <li>Pythagoras' Theorem</li> <li>Angle properties in a polygon-Interior and Exterior angles in a polygon</li> <li>Basic Trigonometry</li> </ul>	<ul> <li>Derive Pythagoras' theorem</li> <li>Use Pythagoras' theorem to find missing sides in right-angled triangles</li> <li>Solve associated problems in other shapes where right-angled triangles exist</li> <li>Deduce whether a triangle is right-angled by considering its sides</li> <li>Find the formula for sum of the angles of any polygon</li> <li>Understand and use the sum of the exterior angles of a polygon</li> <li>Solve problems involving the angles/number of sides in a regular polygon</li> <li>Develop an understanding of the trigonometric ratios</li> <li>Solve problems using trigonometric ratios in right-angled triangles</li> <li>Pythagoras' theorem a<sup>2</sup> + b<sup>2</sup> = c<sup>2</sup>, and the trigonometric ratios, sin θ = opposite/hypotenuse, cos θ = adjacent/hypotenuse, cos θ = adjacent/hypotenuse and tan θ = opposite/adjacent apply them to find angles and lengths in right-angled triangles in two and three dimensional figures</li> <li>know the exact values of sin θ and cos θ for θ = 0°, 30°, 45°, 60° and 90°; know the exact</li> </ul>	<ul> <li>know the formulae for: Pythagoras' theorem, a<sup>2</sup> + b<sup>2</sup> = c<sup>2</sup></li> <li>Use trigonometric ratios to calculate an angle in a right-angled triangle.</li> <li>Find angles of elevation and angles of depression.</li> <li>Use trigonometric ratios to solve problems.</li> <li>Know the exact values of the sine, cosine and tangent of some angles.</li> <li>Investigate how other polygons, starting with quadrilaterals, can be divided into triangles and so deduce the general formula.</li> <li>Following on from investigating exterior angles, they will then solve a series of problems such as finding the number of sides given information about the angles of polygons.</li> <li>Investigate the trigonometric ratios using similar triangles</li> <li>Define and use the cosine, sine and tangent ratios</li> </ul>	
		value of tan $\theta$ for $\theta$ = 0°, 30°, 45° and 60°		
pring 2	<ul> <li>Algebra</li> <li>Rate of Change and graphs</li> <li>Quadratic Graphs</li> </ul>	<ul> <li>Students will be able to:</li> <li>Use linear and quadratic graphs to estimate values of <i>y</i> for given values of <i>x</i></li> <li>Find acceleration and distance from velocity-time graphs.</li> <li>Draw and interpret real-life linear graphs.</li> <li>Find the coordinates of the midpoint of a line segment.</li> <li>Find the gradient and length of a line</li> </ul>	<ul> <li>Identify variables and express relations between variables algebraically and graphically</li> <li>Find approximate solutions to contextual problems from given graphs of a variety of functions including:(e.g. real-life linear graphs)</li> <li>recognise, sketch and interpret graphs of linear functions, quadratic functions, <u>simple</u></li> </ul>	<ul> <li>At the end of each unit there will be a unit test.</li> <li>There will be online assessments for each topic covered.</li> <li>All pupils will be sitting an End of term</li> </ul>
		segment.	cubic functions, the reciprocal function $y = \frac{1/x}{x}$ with $x \neq 0$	an End of term assessment.

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		<ul> <li>Find the equations of lines parallel or perpendicular to a given line.</li> <li>Draw quadratic graphs.</li> <li>Solve quadratic equations using graphs.</li> <li>Identify the line of symmetry of a quadratic graph.</li> <li>Interpret quadratic graphs relating to real-life situations.</li> <li>Draw graphs of cubic functions.</li> <li>Solve cubic equations using graphs.</li> <li>Draw graphs of reciprocal functions.</li> <li>Recognise a graph from its shape.</li> <li>Interpret linear and non-linear real-life graphs.</li> <li>Draw the graph of a circle.</li> </ul>	<ul> <li>plot and interpret graphs <u>(including reciprocal graphs</u>) and graphs of non-standard functions in real contexts to find approximate solutions to problems such as simple kinematic problems involving distance, speed and acceleration</li> </ul>	<ul> <li>Pupils will be assessed additionally as best seen fit by their subject teacher.</li> <li>Mathswatch</li> <li>Group work</li> <li>Class discussions</li> <li>Targeted Questioning</li> </ul>
Summer 1	SSM • Area, Perimeter, Surface Area and Volume	<ul> <li>Students will be able to:</li> <li>Recall and use the formula for the area of a trapezium.</li> <li>Convert between metric units of area.</li> <li>Calculate the maximum and minimum possible values of a measurement.</li> <li>Convert between metric units of volume.</li> <li>Calculate volumes and surface areas of prisms.</li> <li>Calculate the area and circumference of a circle.</li> <li>Calculate area and circumference in terms of π.</li> <li>Calculate the perimeter and area of semicircles and quarter circles.</li> <li>Calculate arc lengths, angles and areas of sectors of circles.</li> <li>Calculate volume and surface area of a cylinder and a sphere.</li> <li>Solve problems involving volumes and surface area of pyramids and cones.</li> </ul>	<ul> <li>identify and apply circle definitions and properties, including: centre, radius, chord, diameter, circumference, tangent, arc, sector and segment</li> <li>know and apply formulae to calculate: area of triangles, parallelograms, trapezia; volume of cuboids and other right prisms (including cylinders)</li> <li>know the formulae: circumference of a circle = 2πr = πd, area of a circle = πr<sup>2</sup>; calculate: perimeters of 2D shapes, including circles; areas of circles and composite shapes; surface area and volume of spheres, pyramids, cones and composite solids</li> <li>calculate arc lengths, angles and areas of sectors of circles</li> </ul>	<ul> <li>All pupils will be sitting an End of term assessment.</li> <li>Pupils will be assessed additionally as best seen fit by their subject teacher.</li> <li>Mathswatch</li> <li>Group work</li> <li>Class discussions</li> <li>Targeted Questioning</li> </ul>

	. Deflect a share in a line, including an	. Identify the type of type of a meeting counted
	Reflect a shape in a line, including on	Identify the type of transformation carried
• Transformation (Review)	coordinate axes	out by comparing an object and image
	Rotate a shape about a center, including on	
	coordinate axes	
	<ul> <li>Describe reflections and rotations.</li> </ul>	<ul> <li>use scale factors, scale diagrams and maps</li> </ul>
	<ul> <li>Enlarge shapes by fractional and negative</li> </ul>	
	scale factors about a centre of enlargement.	
	<ul> <li>Translate a shape using a vector.</li> </ul>	
	<ul> <li>Carry out and describe combinations of</li> </ul>	
	transformations.	• use the standard ruler and compass
	<ul> <li>Draw and use scales on maps and scale</li> </ul>	constructions (perpendicular bisector of a
Constructions	drawings.	line segment, constructing a perpendicular to
	<ul> <li>Solve problems involving bearings.</li> </ul>	a given line from/at a given point, bisecting a
		given angle); use these to construct given
	<ul> <li>Construct triangles using a ruler and</li> </ul>	figures and solve loci problems; know that
	compasses.	the perpendicular distance from a point to a
	<ul> <li>Construct the perpendicular bisector of a</li> </ul>	line is the shortest distance to the line
	line.	
	Construct the shortest distance from a point	
	to a line using a ruler and compasses.	
	<ul> <li>Bisect an angle using a ruler and compasses.</li> </ul>	
	<ul> <li>Construct angles using a ruler and</li> </ul>	
	compasses.	
	<ul> <li>Construct shapes made from triangles using</li> </ul>	
	a ruler and compasses.	
	<ul> <li>Draw a locus.</li> </ul>	
	<ul> <li>Draw a locus.</li> <li>Use loci to solve problems.</li> </ul>	